

2.69  
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$$\frac{1}{\sin x} + \frac{1}{\sin 2x} + \frac{1}{\sin 4x} = 0$$
$$x + \pi k, \frac{\pi}{2}k, \frac{\pi}{4}k$$
$$\boxed{x \neq \frac{\pi}{4}k}$$

ansatz  
Ansatz ✓

$$\sin 2x \sin 4x + \sin x \sin 4x + \sin x \sin 2x = 0$$

$$\sin 2x \sin 4x + \sin x (\sin 4x + \sin 2x) = 0$$

$$\sin 2x \sin 4x + \sin x (2 \sin 3x \cos x) = 0$$

$$\sin 2x \sin 4x + \sin 2x \sin 3x = 0$$

$$\sin 2x (\sin 4x + \sin 3x) = 0$$

Ansatz  
Ansatz

$$\sin 4x = -\sin 3x = \sin(-3x)$$

$$4x = -3x + 2\pi k$$

$$x = \frac{2\pi k}{7}$$

$$\text{Ansatz } \frac{2}{7}k \quad \text{Ansatz } k \quad \text{Ansatz } \frac{k}{7}$$

k ≠ 7n

$$4x = \pi + 3x + 2\pi k$$

$$x = \pi + 2\pi k$$

$$\text{Ansatz } \frac{\pi}{7}$$