

18
(356)

(10 x 3 = 30 points)

$n=1$

$$1^3 = 1 - 3 \quad \checkmark$$

$n=k$

$$1^3 - 2^3 + \dots + (2k-1)^3 = 4k^3 - 3k^2$$

$n=k+1$

$$1^3 - 2^3 + \dots + (2k-1)^3 - (2k)^3 + (2k+1)^3 \stackrel{?}{=} 4(k+1)^3 - 3(k+1)^2$$

$$4k^3 - 3k^2 - (2k)^3 + (2k+1)^3 \stackrel{?}{=} 4(k^3 + 3k^2 + 3k + 1) - 3(k^2 + 2k + 1)$$

$$4k^3 - 3k^2 - 8k^3 + 8k^2 + 12k + 6k + 1 \stackrel{?}{=} 4k^3 + 12k^2 + 12k + 4 - 3k^2 - 6k - 3$$

$$4k^3 + 9k^2 + 6k + 1 = 4k^3 + 9k^2 + 6k + 1$$